

**ENGINEERING MATHS-I**  
**(AM-101, DEC-05)**

**Note:** Section A is compulsory. Attempt any five questions from Section B and C taking at least two questions from each part.

**Section-A**

1. (a) Define the point of inflection for a curve and find (s) of inflection for the curve  
 $y = x^3 + 8x^3 - 270x$
- (b) What do you understand by parametric curves? Give an example of a parametric curve involving two parameters.
- (c) Using parametric equation of a circle, show that the area of circle of radius r is  $\pi r^2$ .
- (d) Find the area of sphere generated by revolving the circle  
 $x^2 + y^2 = r^2$  about x axis
- (e) If  $x = r \cos\theta$  and  $y = r \sin\theta$ , Find  $\frac{\partial(x, y)}{\partial(r, \theta)}$  and  $\frac{\partial(r, \theta)}{\partial(x, y)}$
- (f) Find the equation of normal line to the surface  $xyz = a^3$  at  $P(x_1, y_2, z_1)$
- (g) Evaluate  $\int_0^1 \int_0^1 (x+2) dy dx$
- (h) State De Moivre's theorem and prove it for the most fundamental case.
- (i) Define tangent plane to a sphere and derive the equation of tangent plane taking a general equation of the sphere.
- (j) Define Beta function.

**Section-B**

2. Trace the polar curve  
 $r = a(1 - \cos\theta)$ , where a is +ve constant.
3. Find the area contained between x-axis and one arch of the curve  $y = \cos 3x$ .
4. (a). Verify the Euler's theorem for  
 $f(x, y, z) = 3x^2yz + 3xy^2z + 4z^4$
- (b) If  $u = \sin^{-1}(x - y)$   $x = 3t$ ,  $y = 4t^3$ , find the value of  $\frac{du}{dt}$
5. Use Lagrange's method to find the minimum value of  $x^2 + y^2 + z^2$  subject to the condition  $x+y+z=1$  and  $xyz=1=0$

**Section-C**

6. Show that the plane  $2x-2y+z+12=0$  touches the sphere  $x^2+y^2+z^2-2x+4y+2z-3=0$ . Also find the point of contact.
7. Using double integration, find the area enclosed between the curve  $y^2=x^3$  and  $y=x$
8. Test the following series for uniform convergence  $\sum \frac{\cos n^x}{n^3}$  for  $\pi < x < 2\pi$ .
9. If  $u = \log\left(\tan\left(\frac{\pi}{4} + \frac{\theta}{2}\right)\right)$ , prove that (i)  $\sinh(u) = \tan\theta$       (ii)  $\tanh u = \sin\theta$